

FACULTIES OF ARTS AND SCIENCE
B.A. / B.Sc. I-Semester (CBCS) Examination, December 2016

Subject : Mathematics

Paper – I : Differential Calculus

Time : 3 Hours

Max. Marks: 80

PART – A (5 x 4 = 20 Marks)

(Short Answer Type)

Note : Answer any FIVE of the following questions.

- 1 Expand $f(x) = \log(1 + \sin x)$ by using Maclaurin's theorem.
- 2 Find the c value of Rolle's mean value theorem for the function

$$f(x) = \log\left(\frac{x^2 + ab}{x(a+b)}\right)$$
 on $[a, b]$.
- 3 Evaluate $\lim_{x \rightarrow 0} (\cot x)^{\sin x}$.
- 4 Find the radius of curvature of the curve
 $x = a \cos^3 t, y = b \sin^3 t$ at $t = \pi/4$.
- 5 If $z = \log(u^2 + v)$, $u = e^{x+y^2}$, $v = x + y^2$ then evaluate $2y \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}$
- 6 If $u = \tan^{-1}\left(\frac{y^2}{x}\right)$ then evaluate

$$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$$
- 7 Find the asymptotes of the curve $x^2y^2 - x^2y - xy^2 + x + y + 1 = 0$, which are parallel to coordinate axes.
- 8 Find the envelope of the curve.
 $my + m^2x - 10 = 0$ where m is a parameter.

PART – B (4 x 15 = 60 Marks)

(Essay Answer Type)

Note: Answer ALL the questions.

- 9 (a) (i) $y = a \cos(\log x) + b \sin(\log x)$ then show that
 $x^2 y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$
(ii) Find the coefficient of x^5 in Maclaurin's series expansion of $f(x) = e^x \cos x$.
OR
- (b) (i) State and prove Cauchy's mean value theorem. Hence find 'c' value of Cauchy's mean value theorem for the function $f(x) = e^x, g(x) = e^{-x}$ on $[a, b]$.

